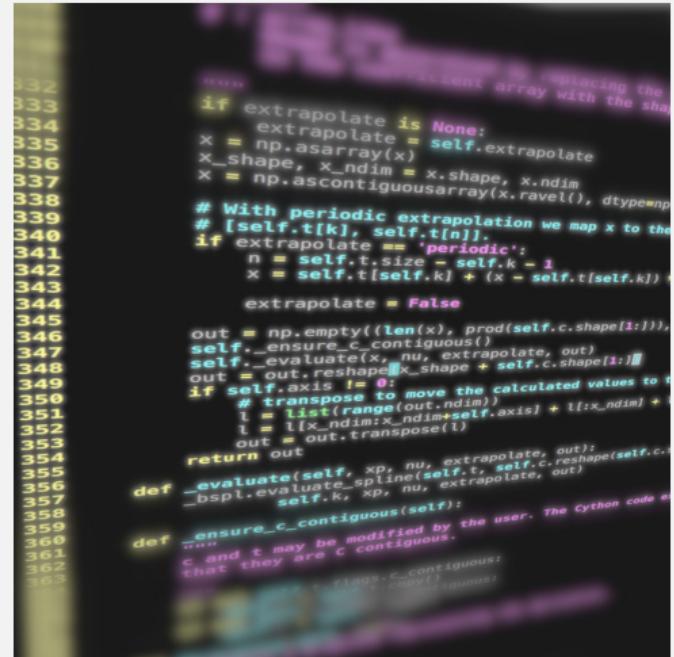


# Programming

## Advanced Programming

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```
332         client array with the shape
333         of the input array
334     if extrapolate is None:
335         extrapolate = self.extrapolate
336     x = np.asarray(x, dtype=np.float64)
337     x_shape, x_ndim = x.shape, x.ndim
338     x = np.ascontiguousarray(x.ravel(), dtype=np.float64)
339     # With periodic extrapolation we map x to the
340     # [self.t[k], self.t[n]].
341     if extrapolate == 'periodic':
342         n = self.t.size - self.k - 1
343         x = self.t[self.k] + (x - self.t[self.k]) *
344             extrapolate = False
345
346     out = np.empty((len(x), prod(self.c.shape[1:])))
347     self._ensure_c_contiguous()
348     self._evaluate(x, nu, extrapolate, out)
349     out = out.reshape(x_shape + self.c.shape[1:])
350     if self.axis != 0:
351         # transpose to move the calculated values to the
352         # right position
353         l = list(range(out.ndim))
354         l[-x_ndim:x_ndim+1] = l[-x_ndim+1:-1]
355         l[-1] = 0
356         out = out.transpose(l)
357
358     def __evaluate(self, xp, nu, extrapolate, out):
359         bsp1.evaluate_spline(self.t, self.c.reshape(self.c.
360                                                 shape[1:]),
361                             self.k, xp, nu, extrapolate, out)
362
363     def __ensure_c_contiguous(self):
364         """"
365         c and t may be modified by the user. The Cython code is
366         not able to check if they are C contiguous.
367         That's why we have to do it here.
368         """
369         if not self.c.flags.c_contiguous:
370             self.c = np.array(self.c, order='C')
```

**Functional  
Programming**

**Lazy  
Evaluation**

**Object-  
oriented  
Programming**

# Functional Programming

## Recursion

A recursive function is a function that calls itself. This example is from Lecture 03.

```
In [1]: def fun(x):
    if len(x) > 1:
        return fun(x[1:])
    return x

fun([1, 2, 3, 4])
```

```
Out[1]: [4]
```

## Functions as objects

In Python everything is an object, including functions:

```
In [2]: def makeList(a, b):
         return [a, b]

myVariable = makeList
```

We can now call the variable that points to the function:

```
In [3]: myVariable(1, 2)

Out[3]: [1, 2]
```

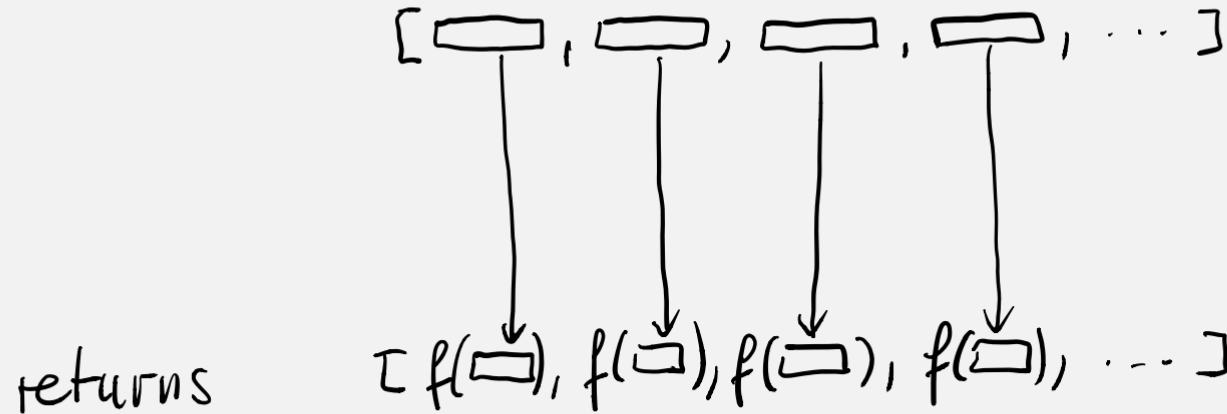
This also allows us to pass functions on to other functions:

```
In [4]: def applyFunction(fun, a, b):
    return fun(a, b)

applyFunction(makeList, 1, 2)
```

```
Out[4]: [1, 2]
```

**Map**       $\text{map}(f, \text{collection})$



# Mapping

Mapping is a very powerful concept:

```
In [5]: def myMapper(f, collection):
    res = list()
    for el in collection:
        res.append(f(el))
    return res

myMapper(str, [1, 2, 3, 4, 5])
```

```
Out[5]: ['1', '2', '3', '4', '5']
```

A `map` function is already implemented in Python:

```
In [6]: map(str, range(1, 6))
```

```
Out[6]: <map at 0x10620d210>
```

```
In [7]: list(map(str, range(1, 6)))
```

```
Out[7]: ['1', '2', '3', '4', '5']
```

An example how `map` can be used in practice:

```
In [8]: import numpy as np
```

```
ary = np.random.random(3)
ary
```

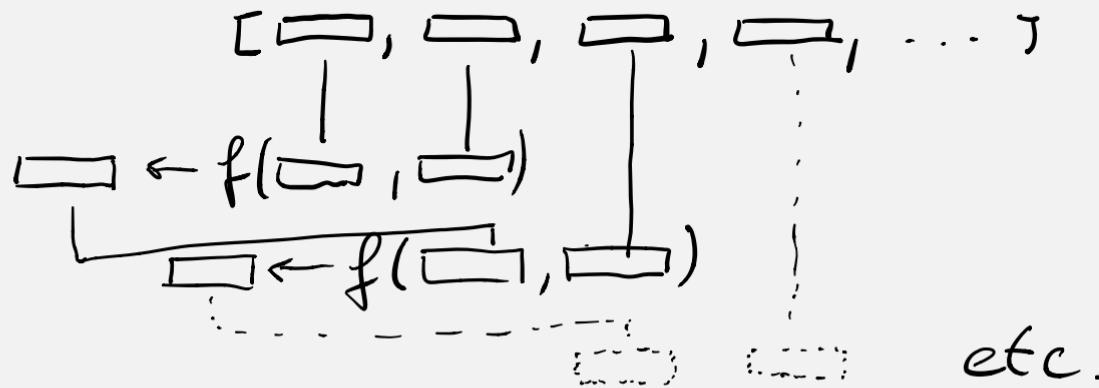
```
Out[8]: array([0.92042043, 0.02694656, 0.8786      ])
```

```
In [9]: list(map(str, ary))
```

```
Out[9]: ['0.9204204259735078', '0.026946558375632645', '0.8786000025464282']
```

**Reduce**     $\text{reduce}(f, \text{collection})$   
               $\vdash f(x, y)$

Iterative reduction of collection through  $f$



Outcome of the last application of  $f$  will be returned

## Reducing

Another very powerful concept:

```
In [10]: from functools import reduce  
  
def addition(a, b):  
    return a + b  
  
reduce(addition, range(10))
```

```
Out[10]: 45
```

## Lambda functions

Lambda functions is just a very convenient way of defining a function in a single line:

```
In [11]: myFunction = lambda x: f'this value is {x}'  
list(map(myFunction, range(3)))
```

```
Out[11]: ['this value is 0', 'this value is 1', 'this value is 2']
```

Here are practical examples, where lambda functions are useful:

```
In [12]: ary = np.random.random(7)
ary
```

```
Out[12]: array([0.24786278, 0.13696996, 0.78356076, 0.84696087, 0.7122092 ,
 0.08724698, 0.38522756])
```

```
In [13]: list(map(lambda x: f'{x:.2f}', ary))
```

```
Out[13]: ['0.25', '0.14', '0.78', '0.85', '0.71', '0.09', '0.39']
```

```
In [14]: reduce(lambda x, y: x + y, range(10))
```

```
Out[14]: 45
```

Lambda functions can contain conditional statements:

```
In [15]: myFun = lambda x: x > 10 and 'larger 10' or 'smaller 10'  
list(map(myFun, range(8, 13)))
```

```
Out[15]: ['smaller 10', 'smaller 10', 'smaller 10', 'larger 10', 'larger 10']
```

```
In [16]: list(filter(lambda x: x > 10, range(8, 13)))
```

```
Out[16]: [11, 12]
```

```
In [17]: lst = [(4, 'a'), (1, 'a'), ('3', 'c'), (1, 'b'), (2, 'd'), (3, 'e')]  
sorted(lst, key = lambda x: x[1])
```

```
Out[17]: [(4, 'a'), (1, 'a'), (1, 'b'), ('3', 'c'), (2, 'd'), (3, 'e')]
```

## List comprehension

```
In [18]: [x for x in range(10)]
```

```
Out[18]: [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

List comprehension with conditional (filter) statement:

```
In [19]: my_list = [1, 'c', 1.0, 'hello world', 'a', 2, 4, 'b', 3.9]  
[x for x in my_list if type(x) == str]
```

```
Out[19]: ['c', 'hello world', 'a', 'b']
```

List comprehension where control variable is further modified prior to output:

```
In [20]: [[x]  for x in my_list if type(x) == str]
```

```
Out[20]: [['c'], ['hello world'], ['a'], ['b']]
```

# Quiz

- True or false?
  - The `map` function applies a function to each element of a collection
  - The `filter` function discards all elements which satisfy a given condition
  - The `reduce` function reduces a collection by summing up its elements
  - List comprehensions enable easy list constructions in one line of code
- What is the result of the following expressions?
  - `list(map(lambda x: x*x-x, range(5)))`
  - `list(filter(lambda x: x%2 == 1, range(10)))`
  - `reduce(lambda x,y: x-y, range(5,0,-1))`
  - `[x-1 for x in range(10) if x%2 == 1]`

# Quiz

## ► True or false?

- The `map` function applies a function to each element of a collection true
- The `filter` function discards all elements which satisfy a given condition false
- The `reduce` function reduces a collection by summing up its elements false
- List comprehensions enable easy list constructions in one line of code true

## ► What is the result of the following expressions?

- `list(map(lambda x: x*x-x, range(5)))` [0, 0, 2, 6, 12]
- `list(filter(lambda x: x%2 == 1, range(10)))` [1, 3, 5, 7, 9]
- `reduce(lambda x,y: x-y, range(5,0,-1))` -5
- `[x-1 for x in range(10) if x%2 == 1]` [0, 2, 4, 6, 8]

**Functional  
Programming**

**Lazy  
Evaluation**

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oriented  
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# Lazy Evaluation

Lazy evaluation means that code statements are not executed until their results are really needed.

List comprehensions are turned into generators by using the round brackets.

```
In [21]: ([x]  for x in my_list if type(x) == str)
```

```
Out[21]: <generator object <genexpr> at 0x10a1a2a50>
```

Using the `next()` function, the currently iterated element of a generator can be retrieved.

```
In [22]: my_gen = ([x]  for x in my_list if type(x) == str)
          next(my_gen)
```

```
Out[22]: ['c']
```

In each call of `next()`, a generator advances its pointer to the current element and returns it, unless the last element has been already reached. In that case, a `StopIteration` exception is thrown.

```
In [23]: print(next(my_gen))
          print(next(my_gen))
          print(next(my_gen))
```

```
['hello world']
['a']
['b']
```

```
In [24]: my_gen = ([x]  for x in my_list if type(x) == str)

try:
    while True:
        print(next(my_gen))
except StopIteration:
    pass
```

```
[ 'c' ]
[ 'hello world' ]
[ 'a' ]
[ 'b' ]
```

Python uses lazy evaluation wherever possible:

```
In [25]: rng = range(1, 6)
print(rng)
```

```
map_generator = map(str, rng)
print(map_generator)
```

```
range(1, 6)
<map object at 0x10a1a4c10>
```

```
In [26]: from itertools import repeat
map(str, repeat(1))
```

```
Out[26]: <map at 0x107efc550>
```

You can create own generator using the `yield` command to return intermediate results in a function.

```
In [27]: def myMapper(fun, collection):
    for el in collection:
        yield fun(el)
    return res
```

```
my_gen = myMapper(str, repeat(1))
my_gen
```

```
Out[27]: <generator object myMapper at 0x10625c450>
```

To demonstrate the power of lazy evaluation, a mapping has been applied to an infinite sequence (`repeat(1)`). You can obtain the first `x` elements of a sequence using another generator function called `islice`:

```
In [28]: from itertools import islice
list(islice(my_gen, 10))
```

```
Out[28]: ['1', '1', '1', '1', '1', '1', '1', '1', '1', '1']
```

It is important to understand that generators can only be iterated over once:

```
In [29]: map_generator = map(str, range(1, 6))
list(map_generator)
```

```
Out[29]: ['1', '2', '3', '4', '5']
```

```
In [30]: list(map_generator)
```

```
Out[30]: []
```

# Quiz

## True or false?

- Lazy Evaluation makes it possible to retrieve elements from an infinite sequence
- Generators can be iterated over an arbitrary number of times
- `range`, `map` and `filter` return generators

# Quiz

## True or false?

- Lazy Evaluation makes it possible to retrieve elements from an infinite sequence true
- Generators can be iterated over an arbitrary number of times false
- `range`, `map` and `filter` return generators true

# Summary

- ❖ Functional programming
  - Map, reduce, ...
  - Lambda functions
  - List comprehension
- ❖ Lazy evaluation
  - Generators and iterators